

# Small Aperture, Low SNR Pulsar Detection

Peter East

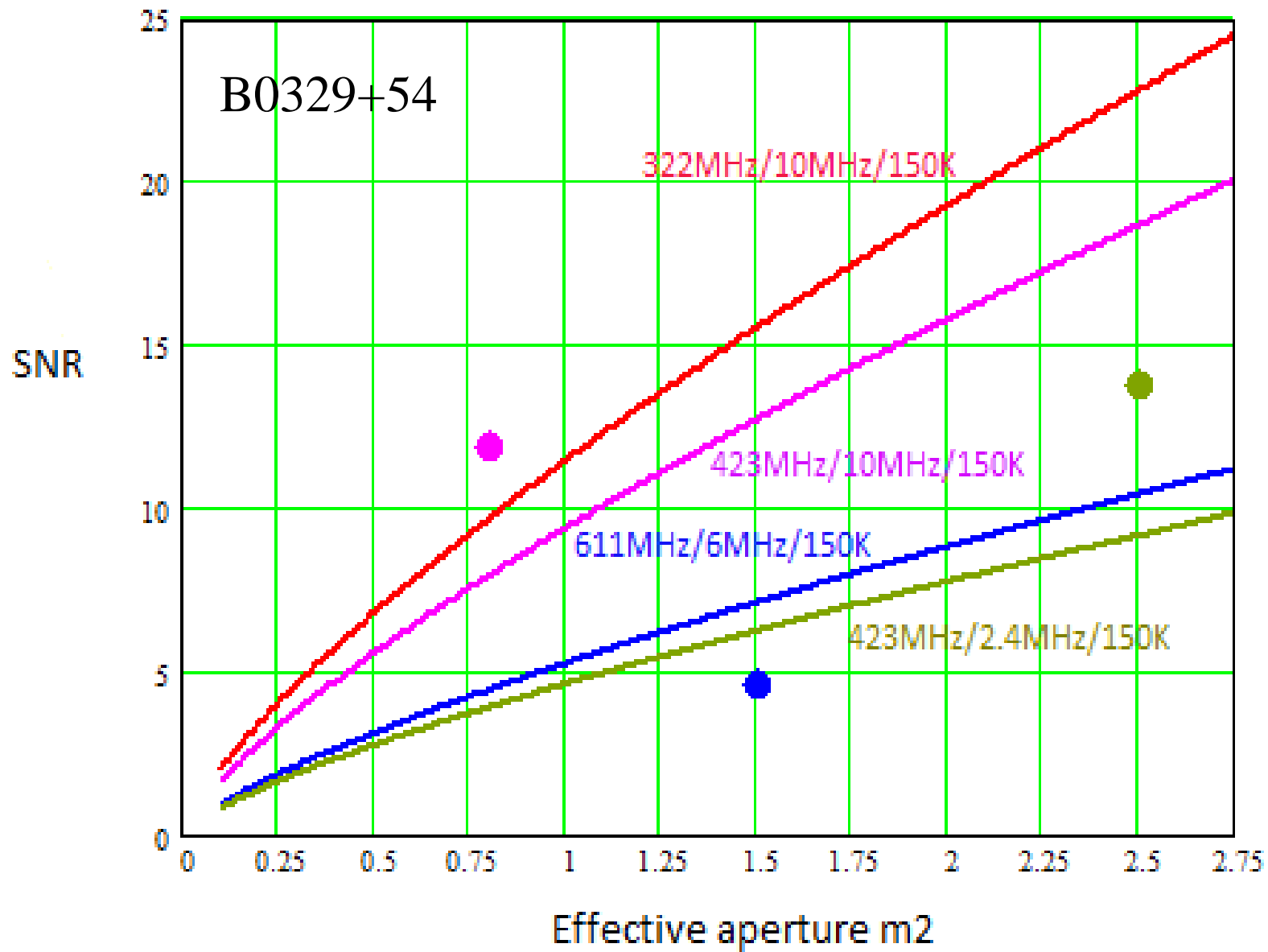
[www.y1pwe.co.uk/RAProgs/Pulsars.html](http://www.y1pwe.co.uk/RAProgs/Pulsars.html)

# Introduction

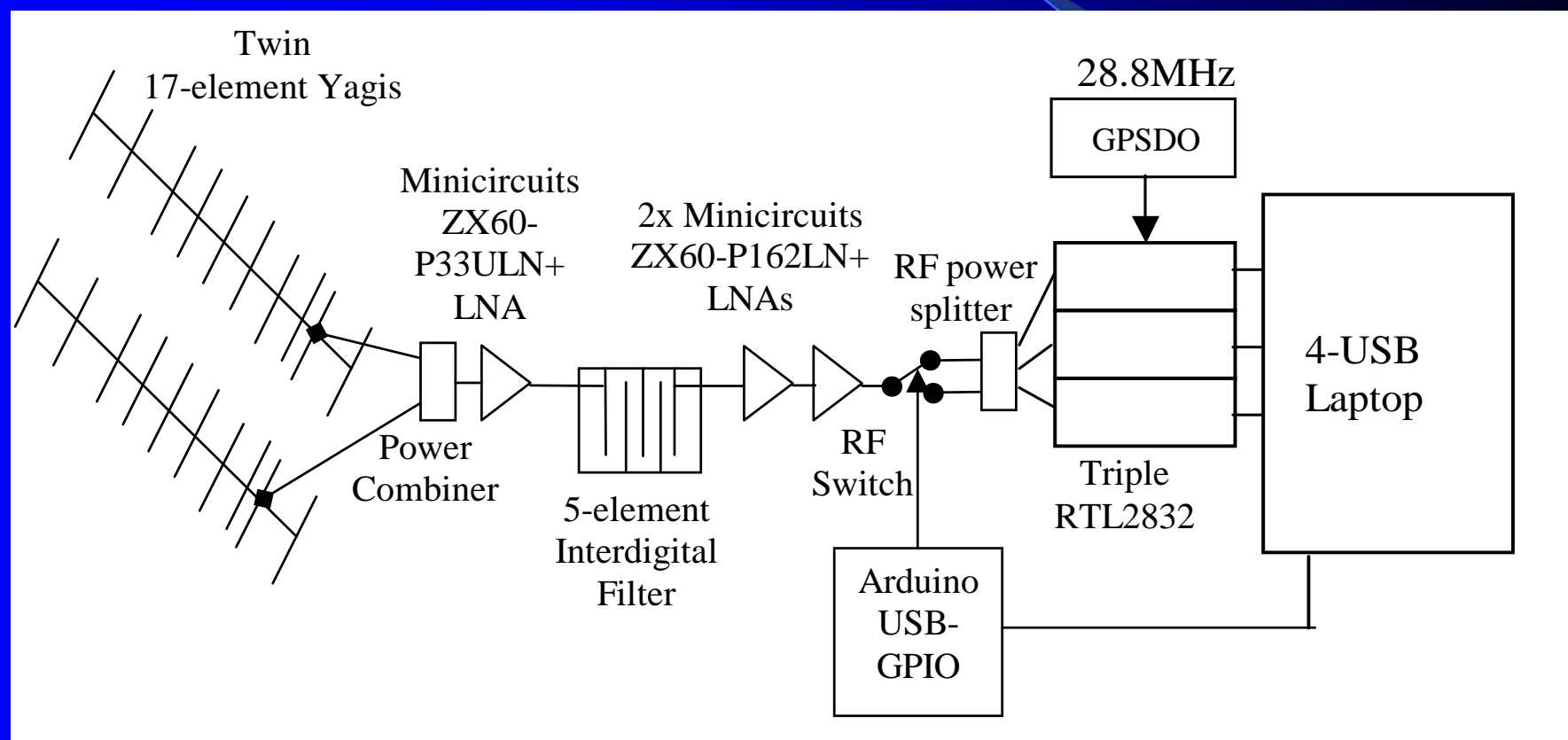
- Background
- Key System Drivers
- Low SNR Tests
- Conclusions

# LK Radiometer Equation

$$SNR = \frac{S_p A_e \sqrt{n_p t_{\text{int}} \Delta f}}{2\beta k_b T_{\text{sys}}} \sqrt{\frac{P - W}{W}}$$



# Mini Pulsar Radio Telescope



# System Temperature - $T_{SYS}$

Receiver noise  
power with Antenna..

1. Connected:  $P_{AC}$
2. Feed O/C:  $P_{OC}$
3. Feed matched:  $P_{ML}$

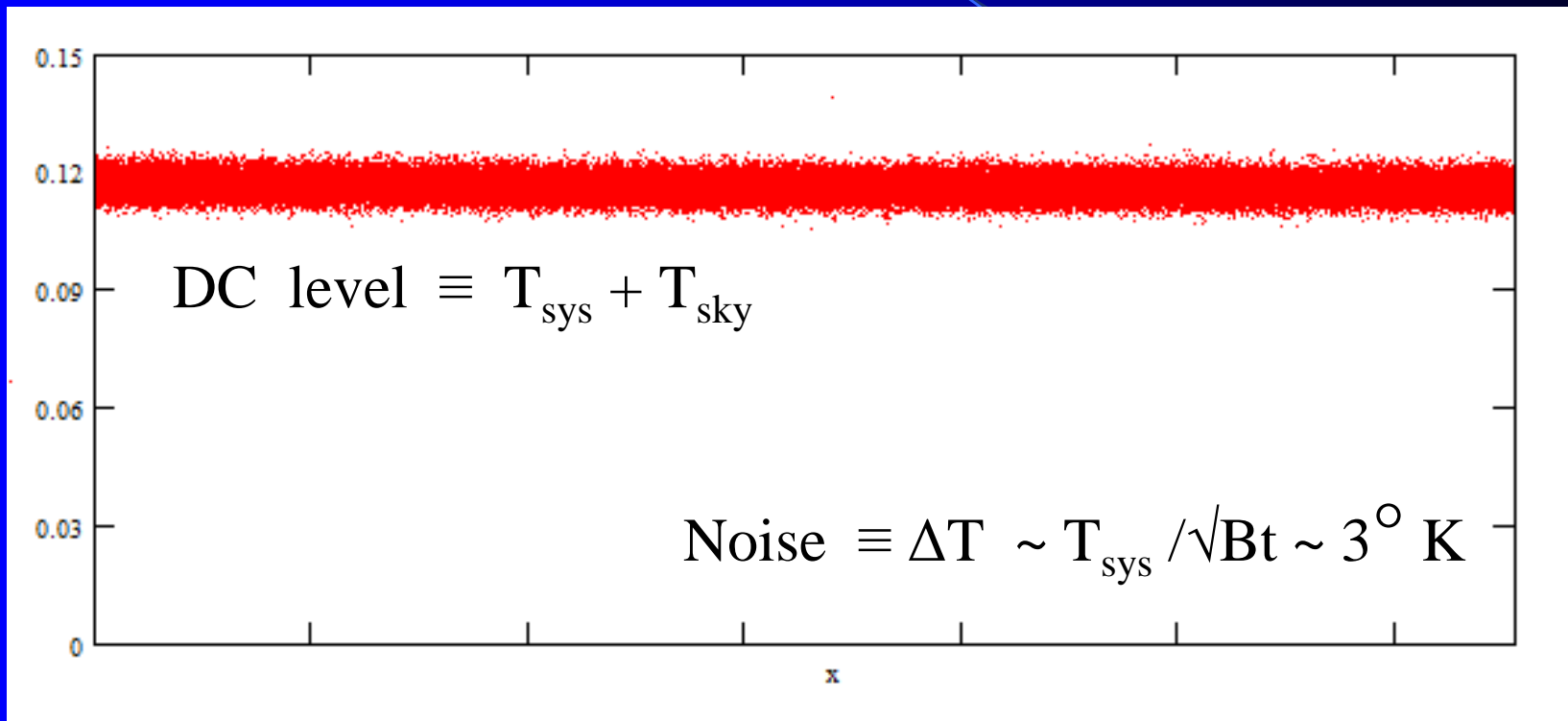
$$\frac{P_{OC}}{P_{ML}} = \frac{T_{RX}}{T_{RX} + 290}$$

$$T_{RX} = T_{LNA} + T_{Losses}$$

$$\frac{P_{AC}}{P_{OC}} = \frac{T_{SYS}}{T_{RX}}$$

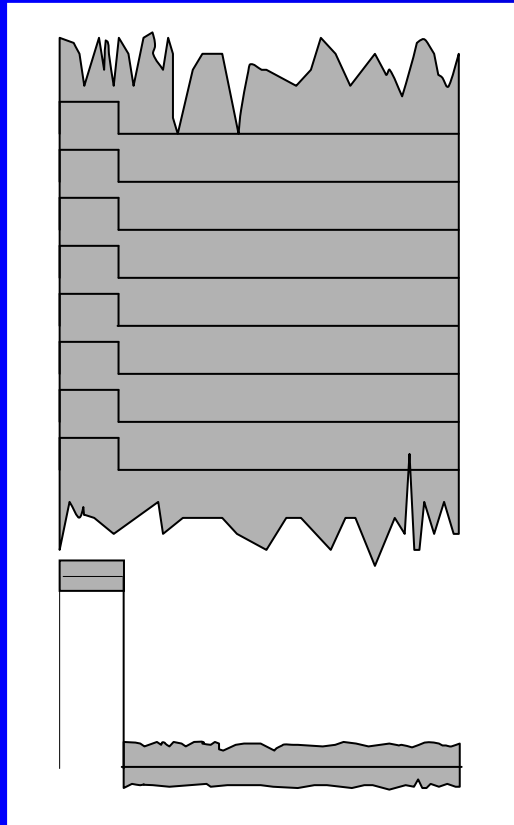
$$T_{SYS} = T_{RX} + T_{SKY} + T_{Antenna}$$

# Detected Video



$$B = 2.4\text{MHz}, t = 1\text{ms}, \text{ and, } (T_{\text{sys}} + T_{\text{sky}}) / \Delta T = 50$$

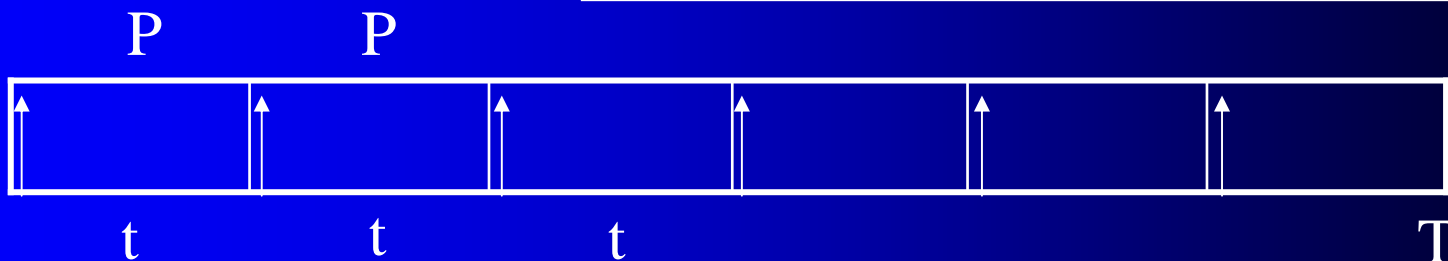
# Folding Algorithm



- \* Pulse adds linearly
- \* Noise adds as square root
- \* SNR improves as  $\sqrt{\text{Folds} = F}$

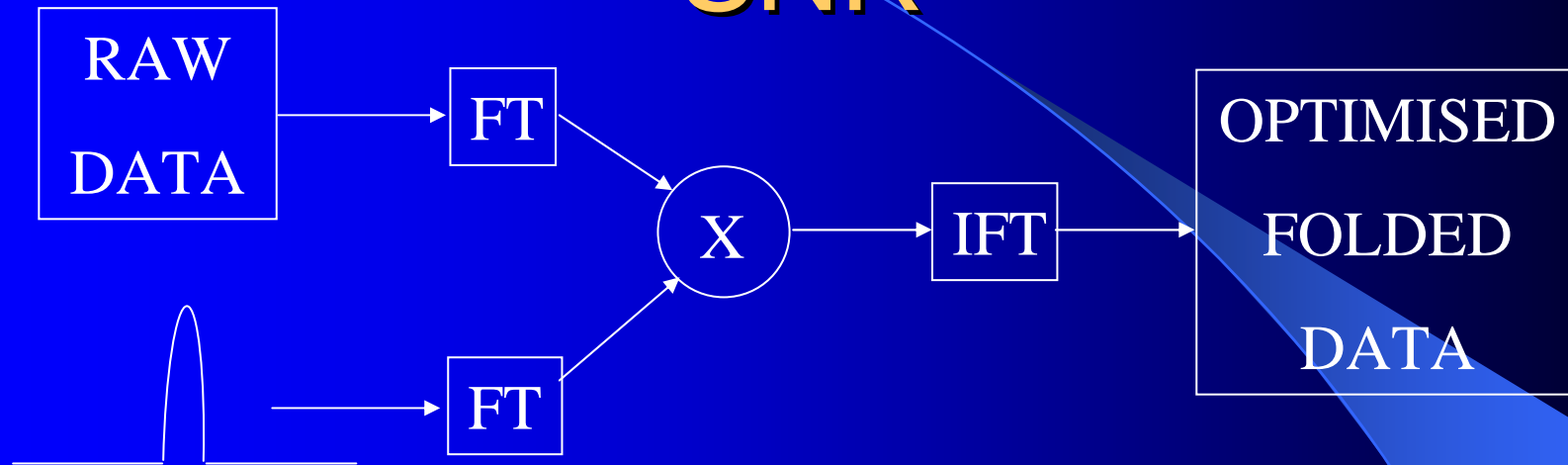
$$\text{SNR} = \sqrt{(FP\Delta f / N)} \times T_p / T_{\text{sys}}$$

- Optimum bins  $N = \text{Period} / \text{Pwidth}$
- B0329:  $T_p \sim 0.03^\circ\text{K}/\text{m}^2/\text{pol}$



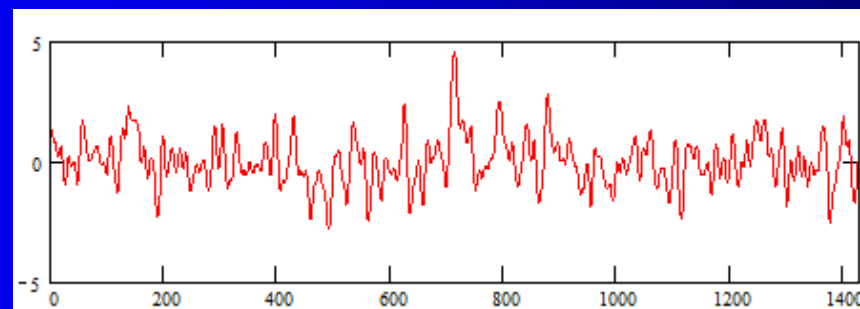
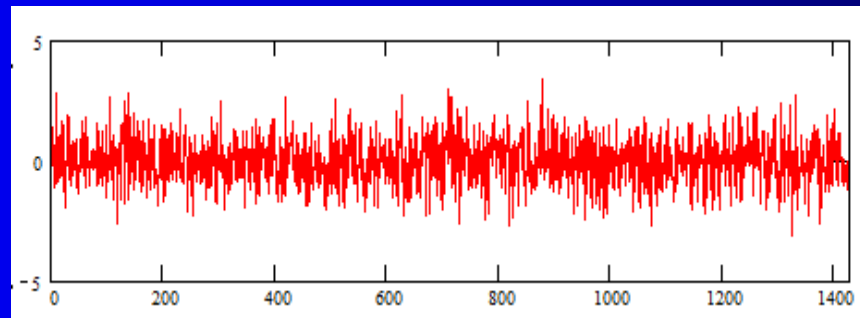


# Matched Filter - optimises SNR



For B0329

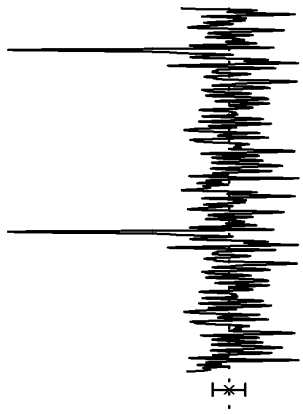
$$\frac{P - W}{W} \approx 109$$



# Finding and Validating

- **Strong signal** - Presto Plot
- **Weak signal** - exploit pulsar characteristics
  1. Correct period – TEMPO + GPS/Rubidium DO
  2. Check pulse width – Matched filter peak
  3. Two-period fold correlation.
  4. Two-section fold correlation
  5. Multi-band correlation.
  6. Period search peak – profile, offset and pulse width
  7. P-dot search peak – profile, offset and pulse width
  8. Dispersion search peak – amplitude and pulse width

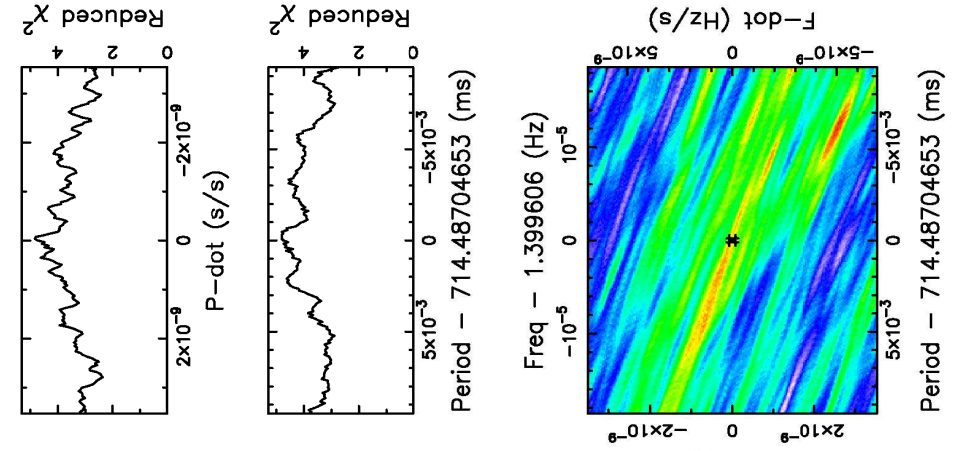
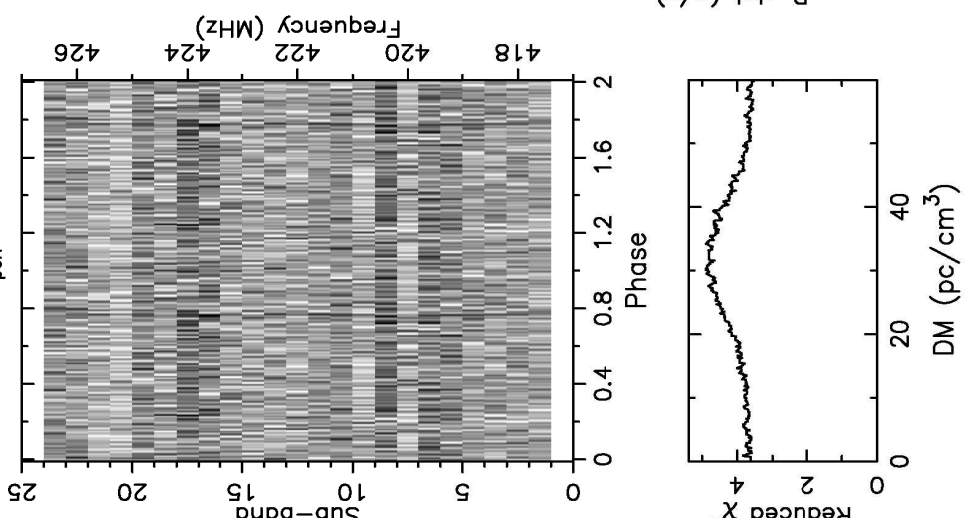
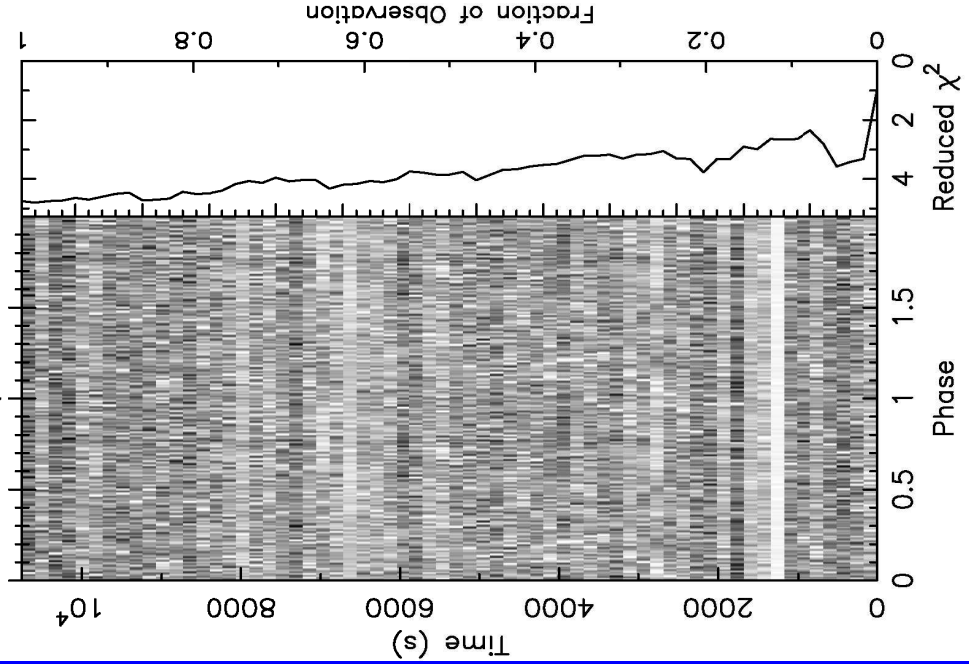
2 Pulses of Best Profile



Candidate: 1.40Hz\_Cand  
 Telescope: Unknown  
 Epoch<sub>topo</sub> = 58300.40419000000  
 Epoch<sub>bary</sub> = N/A  
 T<sub>sample</sub> = 0.0005  
 Data Folded = 21504000  
 Data Avg = 3170  
 Data StdDev = 303.8  
 Profile Bins = 500  
 Profile Avg = 1.363e+08  
 Profile StdDev = 6.301e+04

Search Information  
 RA<sub>J2000</sub> = 03:32:59.3700 DEC<sub>J2000</sub> = 54:34:43.5700  
 Folding Parameters  
 DOF<sub>eff</sub> = 443.35  $\chi^2_{red} = 4.745$  P(Noise) < 6.11e-240 (33.1 $\sigma$ )  
 Dispersion Measure (DM; pc/cm<sup>3</sup>) = 26.974  
 P<sub>topo</sub> (ms) = 714.48705(11) P<sub>bary</sub> (ms) = N/A  
 P<sub>dot\_topo</sub> (s/s) = 0.0(7.6)x10<sup>-11</sup> P<sub>dot\_bary</sub> (s/s) = N/A  
 P<sub>ddot\_topo</sub> (s/s<sup>2</sup>) = 0.0(4.6)x10<sup>-14</sup> P<sub>ddot\_bary</sub> (s/s<sup>2</sup>) = N/A

Binary Parameters  
 P<sub>orb</sub> (s) = N/A e = N/A  
 a<sub>1</sub>sin(i)/c (s) = N/A  $\omega$  (rad) = N/A  
 T<sub>peri</sub> = N/A

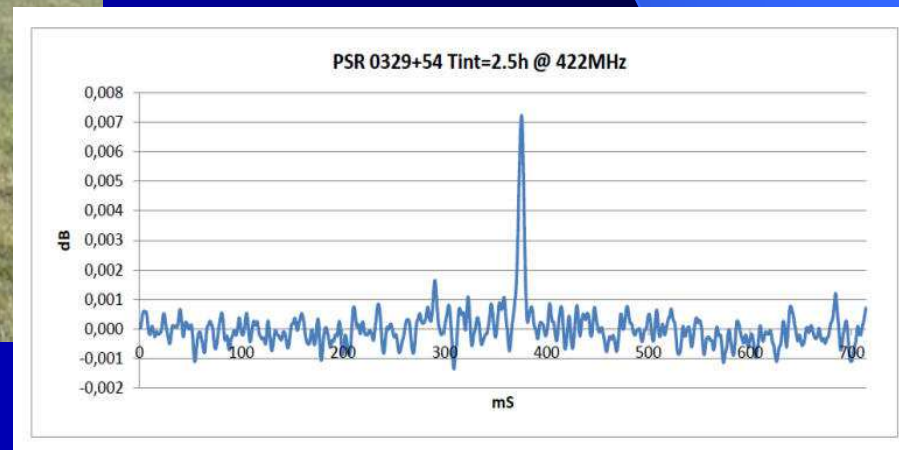


Andrea Dell'Immagine - Italy  
422MHz + 2.4MHz RTL+ 3Hrs  
2x2x2m 3D corner reflector antenna



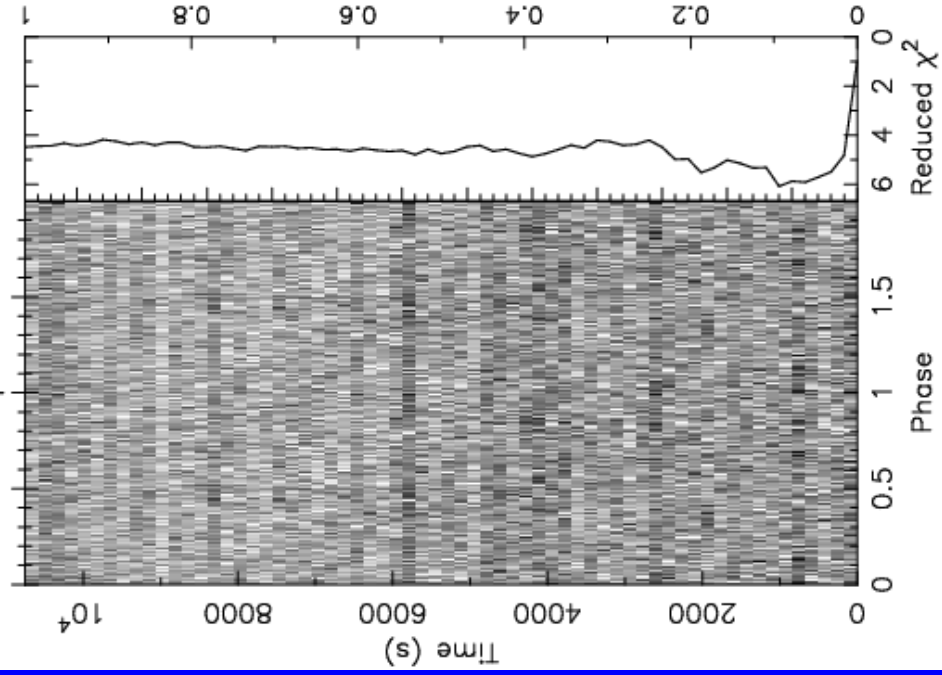
Automatic Daily  
Observatory  
2.5m<sup>2</sup> Aperture

SNR = 11.5

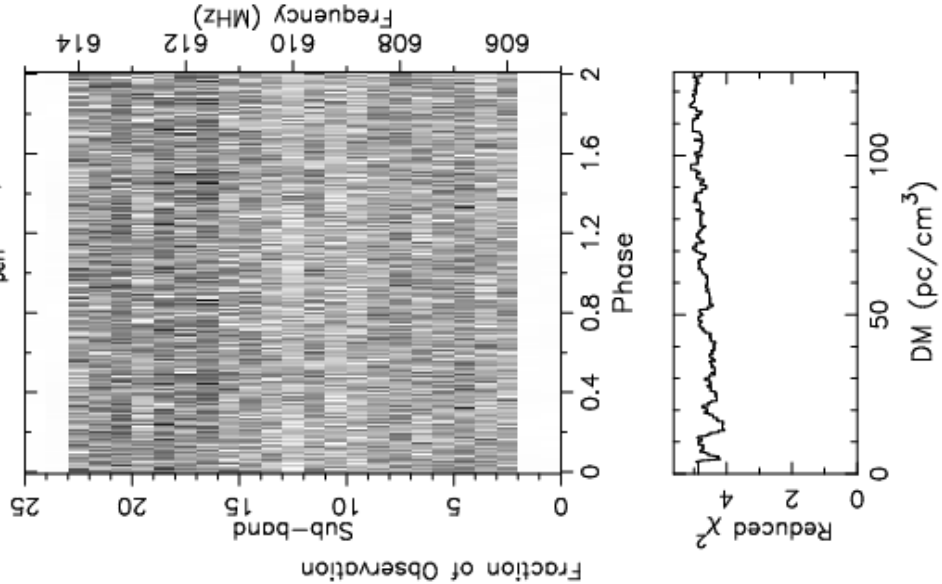


<http://iw5bhy.altervista.org/>

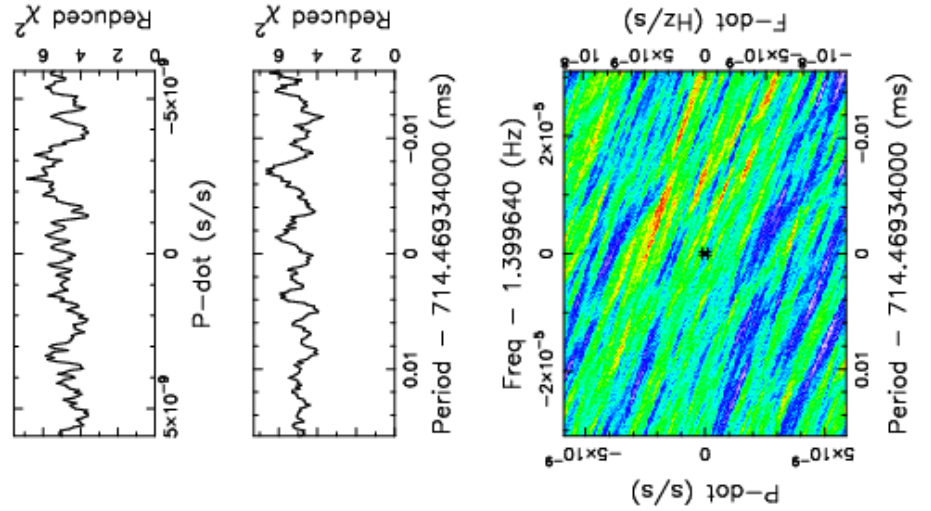
2 Pulses of Best Profile



Candidate: 714.47ms\_Cand  
 Telescope: Unknown  
 Epoch<sub>topo</sub> = 58332.22222222200  
 Epoch<sub>bary</sub> = N/A  
 T<sub>sample</sub> = 0.0005  
 Data Folded = 21504000  
 Data Avg = 3189  
 Data StdDev = 221.9  
 Profile Bins = 300  
 Profile Avg = 2.285e+08  
 Profile StdDev = 5.942e+04



Search Information  
 RA<sub>J2000</sub> = 03:32:59.3700  
 DEC<sub>J2000</sub> = 54:34:43.5700  
 Folding Parameters  
 DOF<sub>eff</sub> = 277.98  
 $\chi^2_{red} = 4.491$   
 $P(\text{Noise}) < 7.05e-132$  (24.4 $\sigma$ )  
 Dispersion Measure (DM; pc/cm<sup>3</sup>) = 26.067  
 P<sub>topo</sub> (ms) = 714.46934(15)  
 P<sub>bary</sub> (ms) = N/A  
 P<sub>topo</sub> (s/s) = 0.0(1.0)x10<sup>-10</sup>  
 P<sub>bary</sub> (s/s) = N/A  
 P<sub>topo</sub> (s/s<sup>2</sup>) = 0.0(6.3)x10<sup>-14</sup>  
 P<sub>bary</sub> (s/s<sup>2</sup>) = N/A  
 Binary Parameters  
 P<sub>orb</sub> (s) = N/A  
 a<sub>1</sub>sin(i)/c (s) = N/A  
 T<sub>peri</sub> = N/A  
 e = N/A  
 ω (rad) = N/A



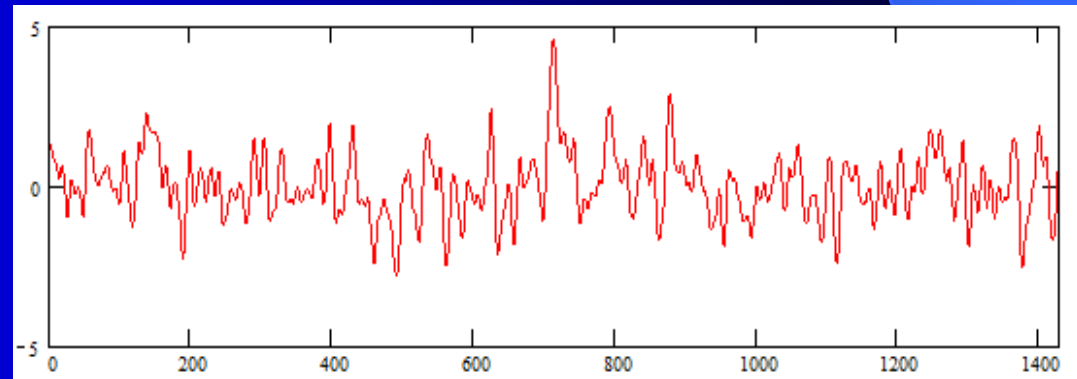
# 611MHz + 6MHz (3x2.4MHz) + 2Hrs Twin 2.5m Yagis



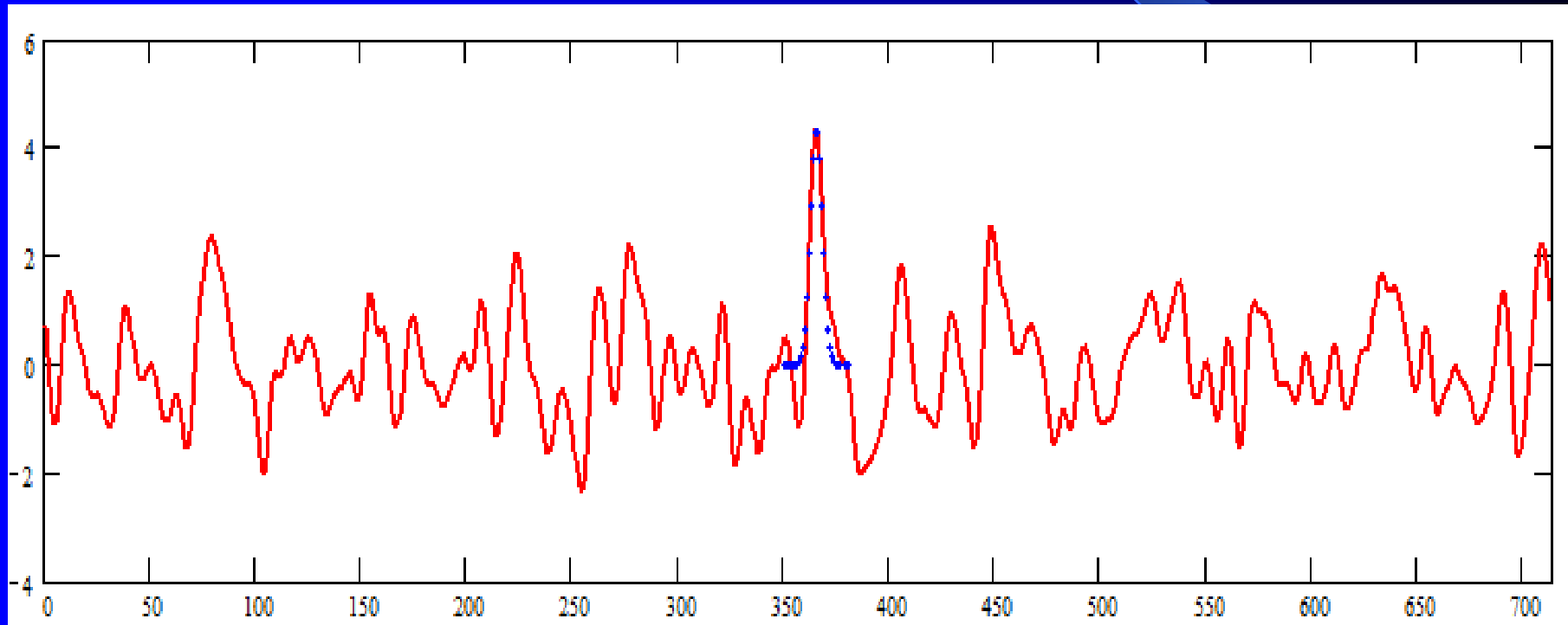
Minimal Affordable System  
1.5m<sup>2</sup> aperture

B0329+54 Pulsar  
period: 714.4816893ms

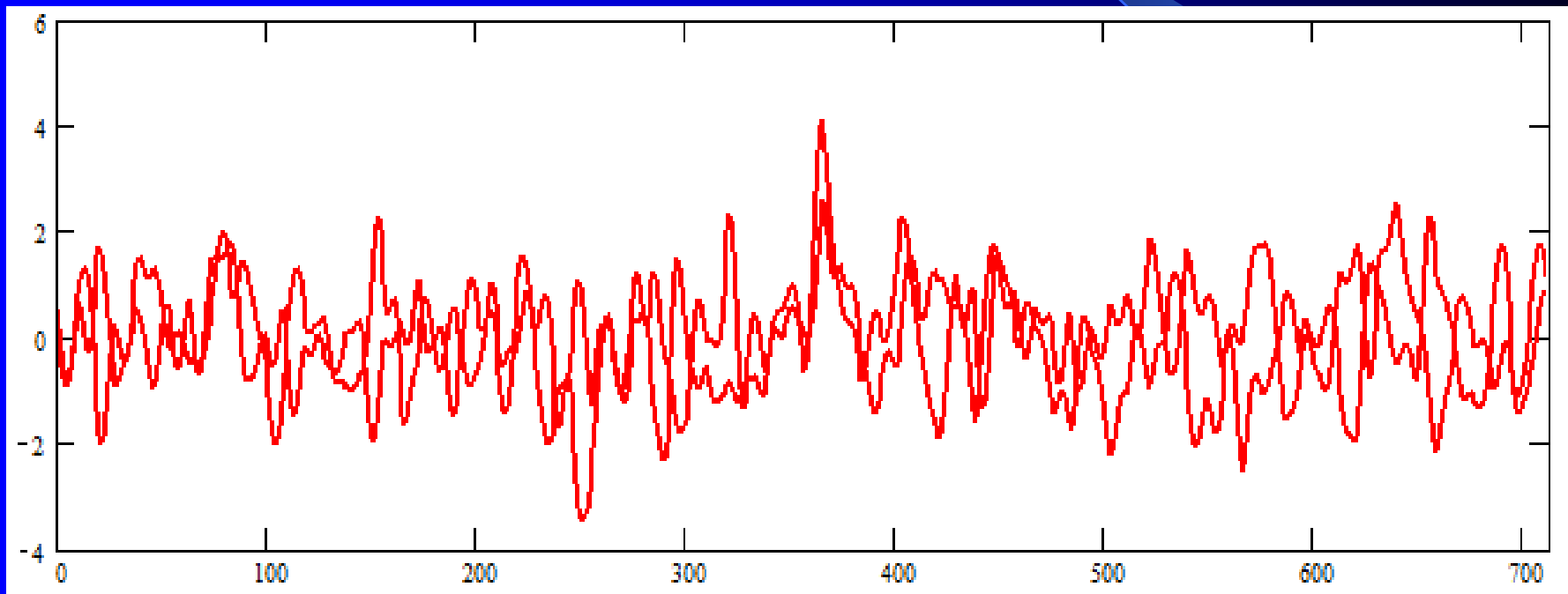
SNR = 4.5



# B0329 Tests 1,2. Period/Pulse Width Check

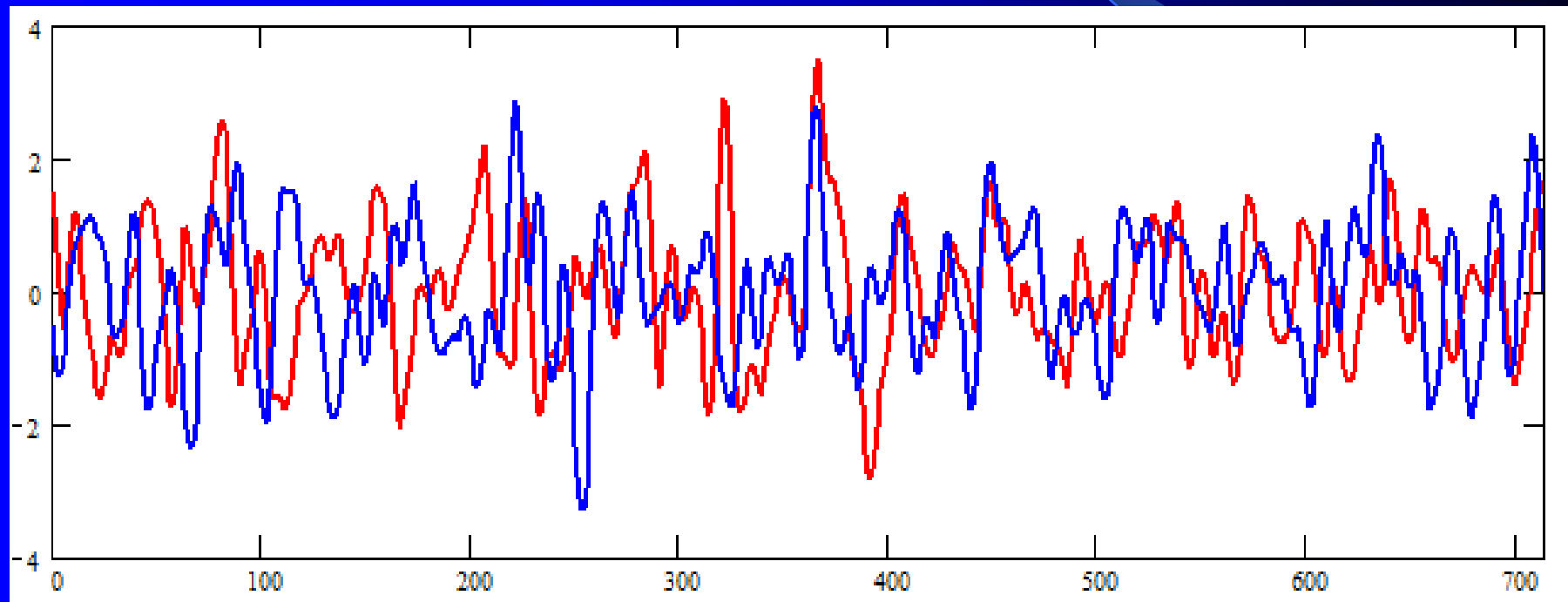


# Test 3. 2-Period Fold - 2 sections overlaid

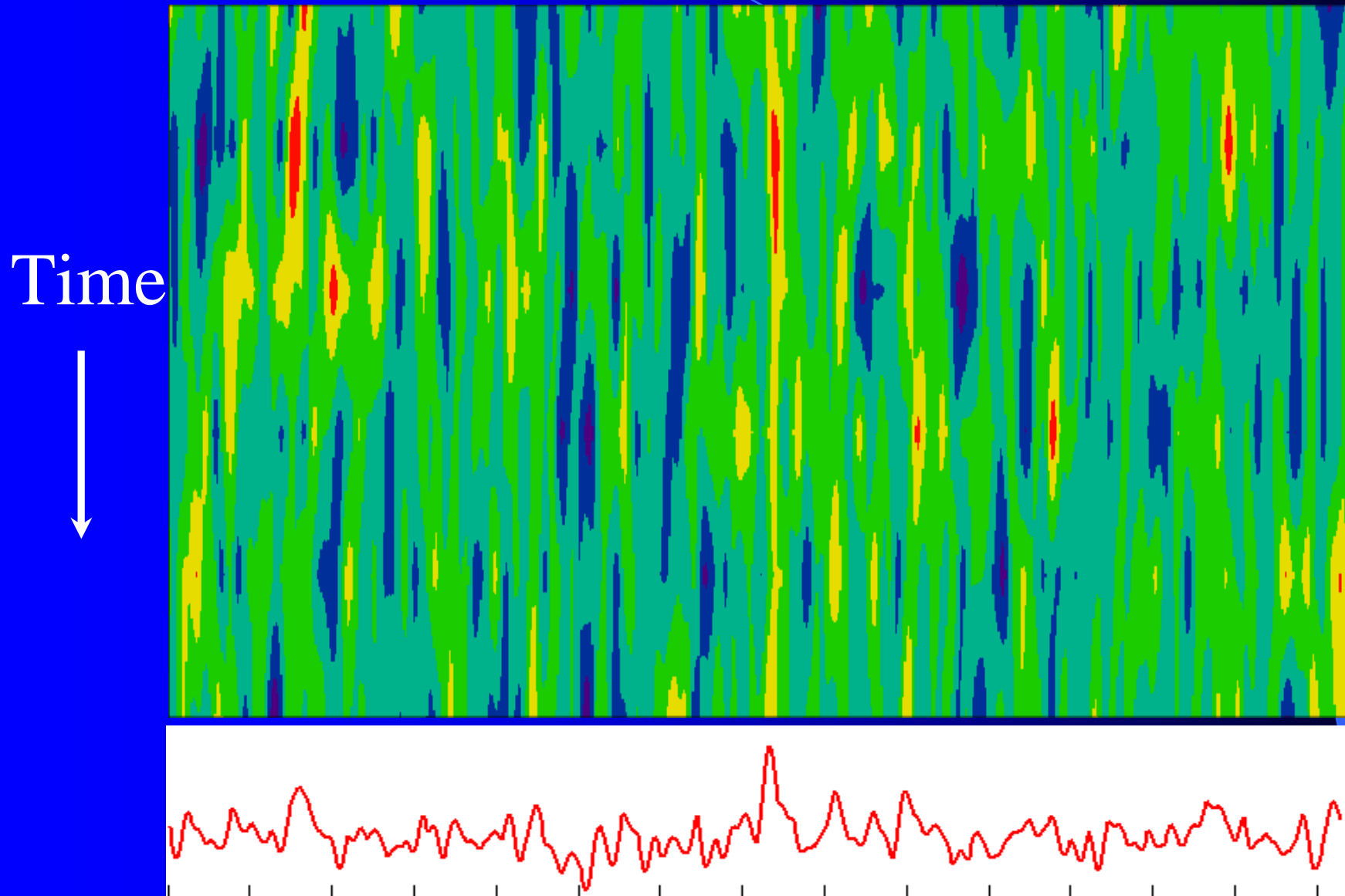




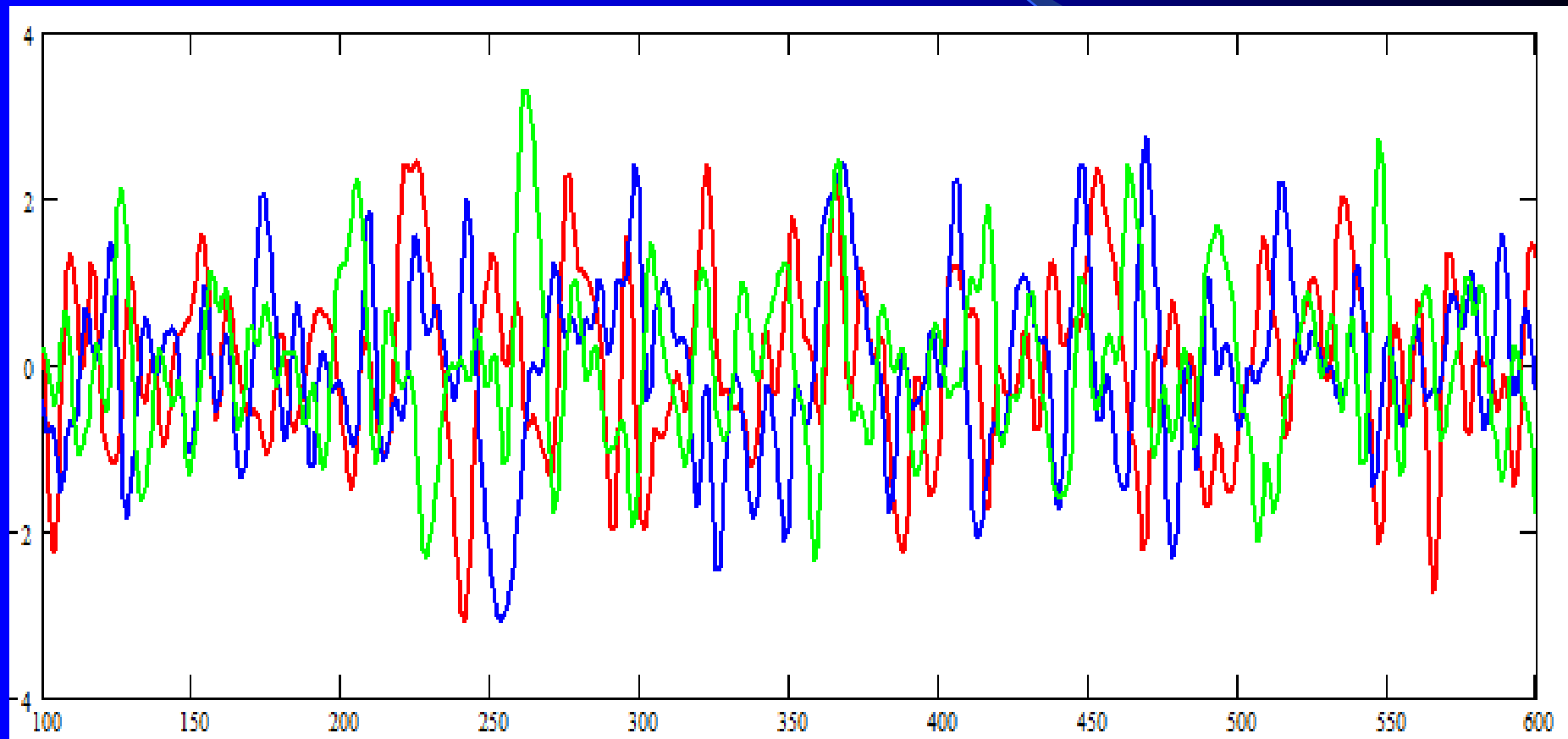
# Test 4. Half File Correlation



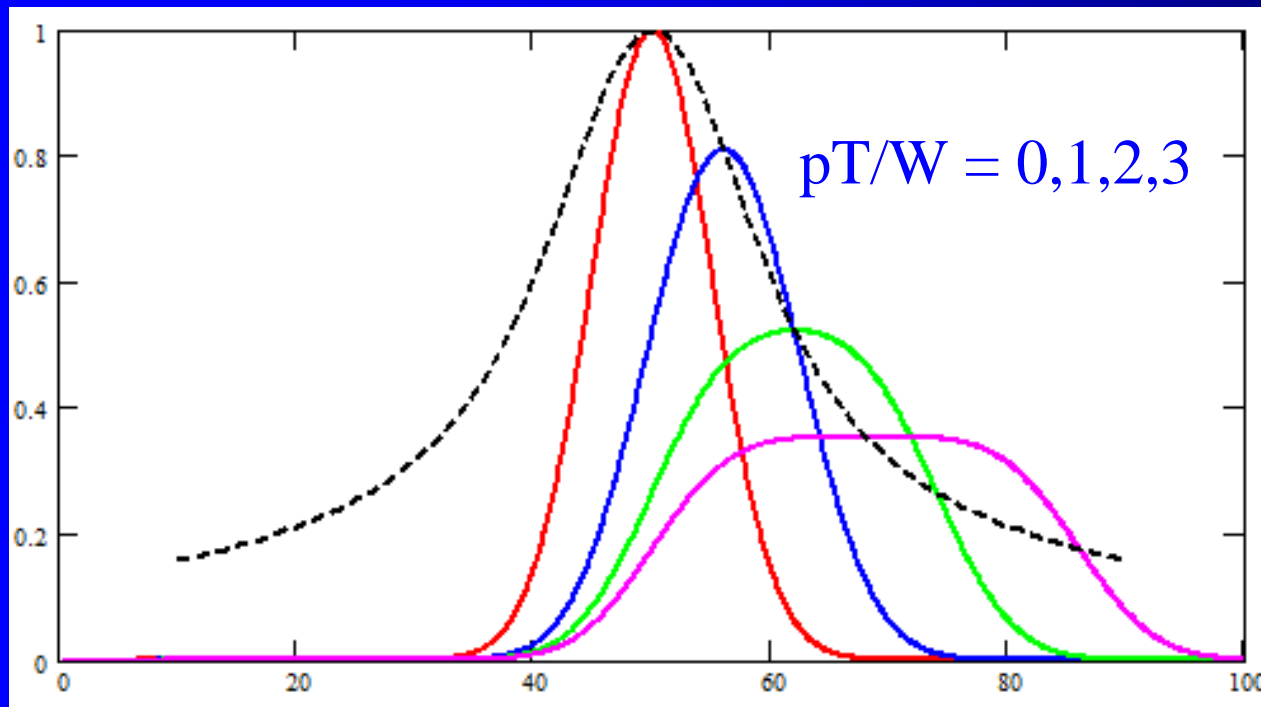
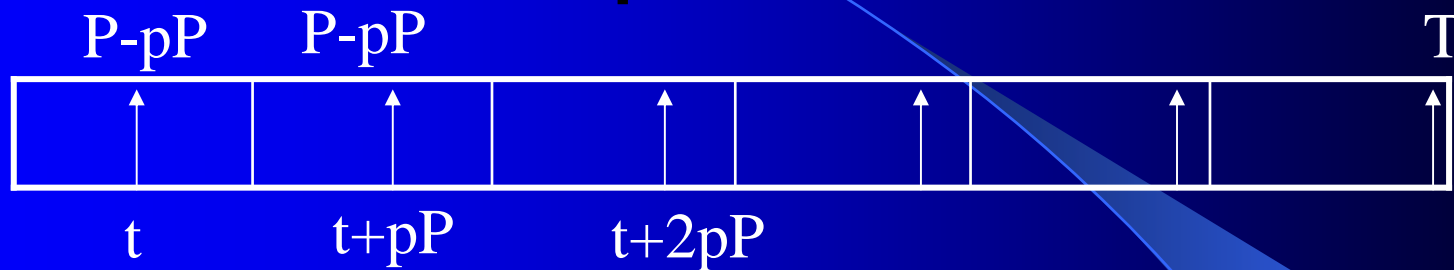
# Test 4. cont'd. Falling Raster



# Test 5. Sub-Band Correlation



# Test 6. Period Search Properties

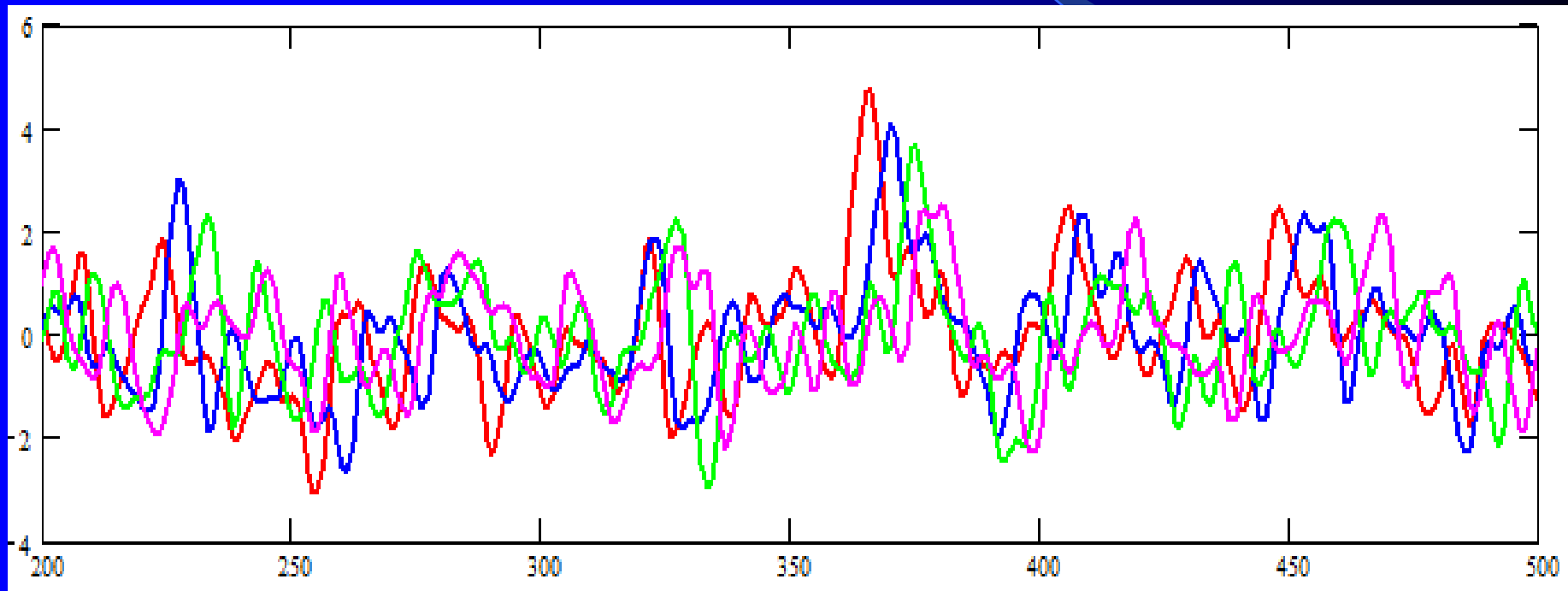


New Width:  $pT$   
 New Peak:  $-pT/2$

Example;  $T=7000s$   
 $p = -1ppm$ ,  $P=700ms$   
 Peak shift =  $+3.5ms$

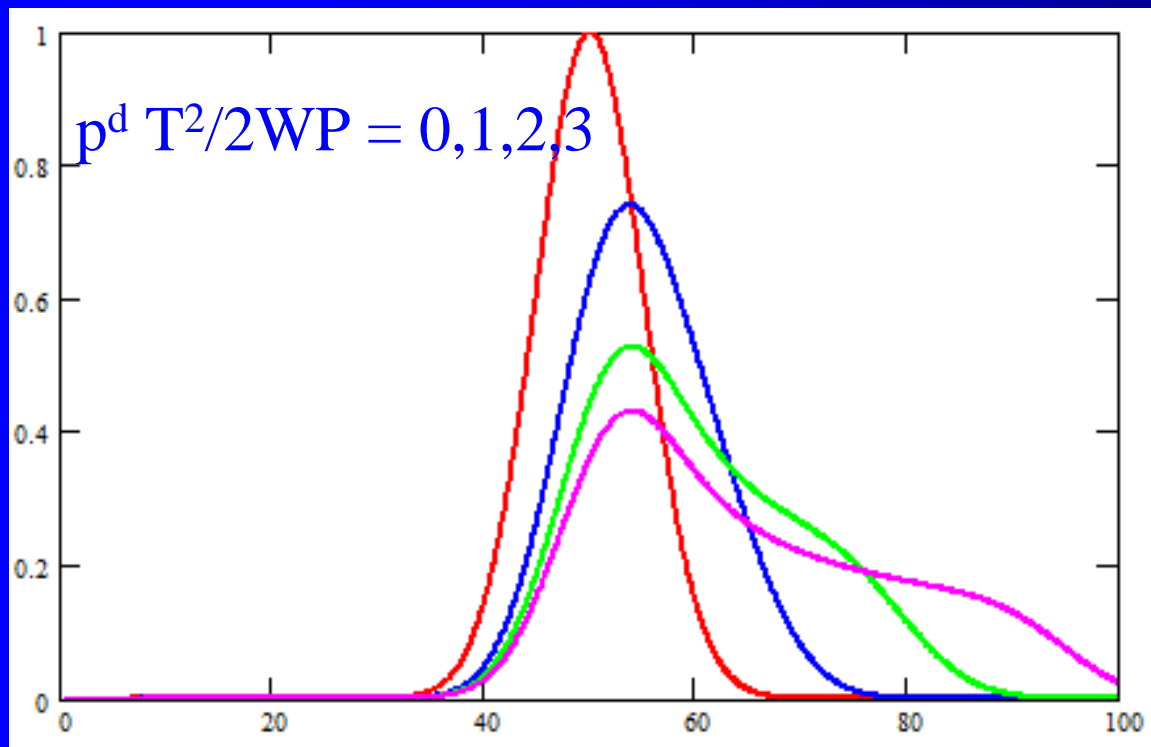
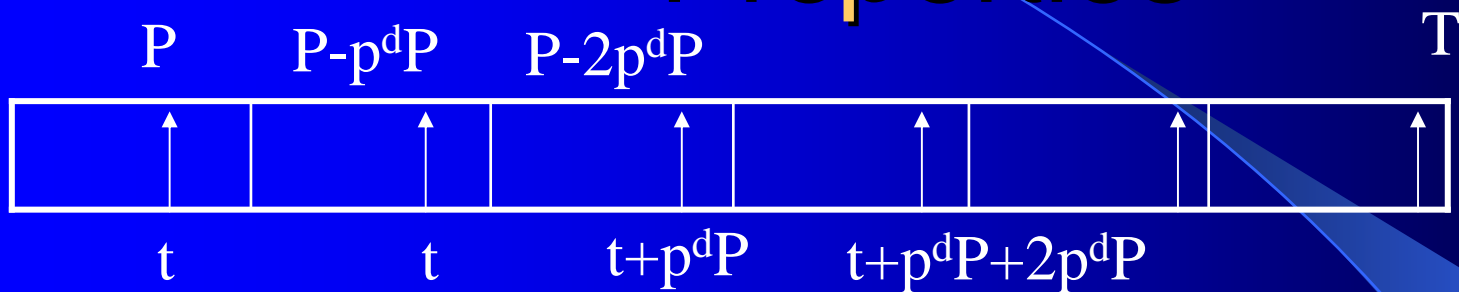
Half height,  $p=2W/T$

# Test 6 cont'd. Period Search Data



$p = 0, -1, -2, -3 \text{ ppm}$

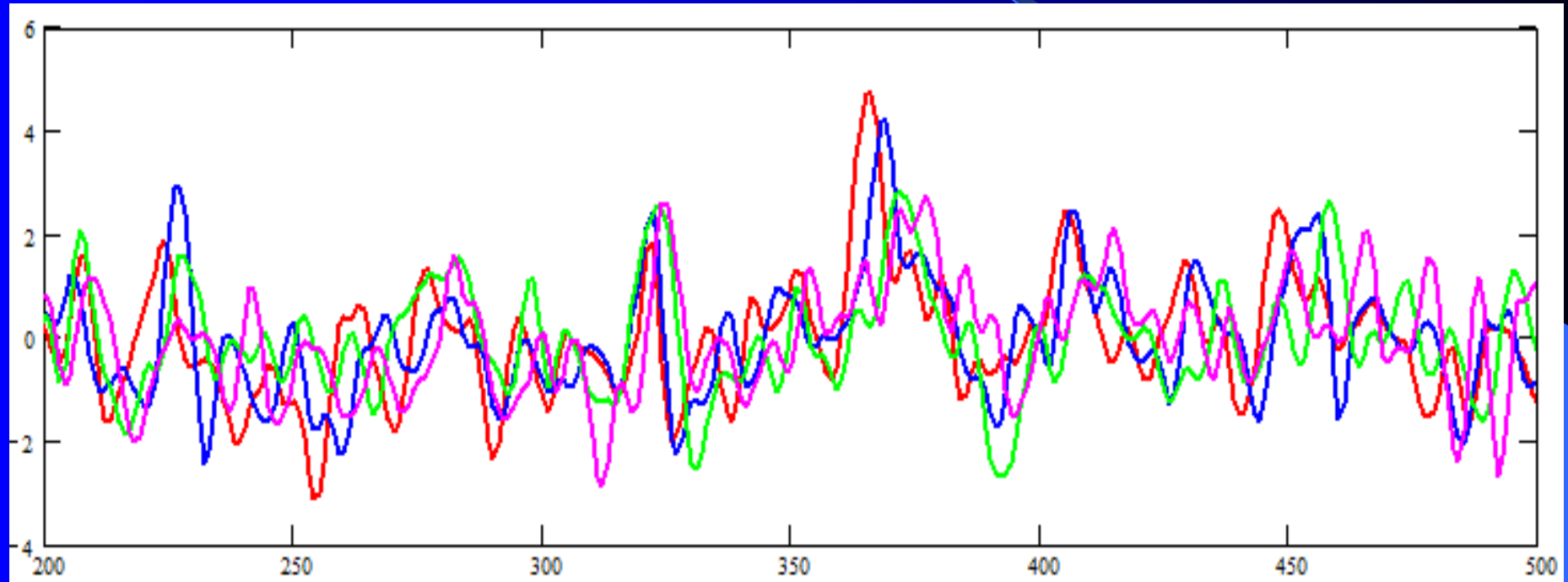
# Test 7. $p$ -dot ( $\delta P/P$ ) Search Properties



For small  $p^d$   
New Width:  $p^d T^2 / 2P$

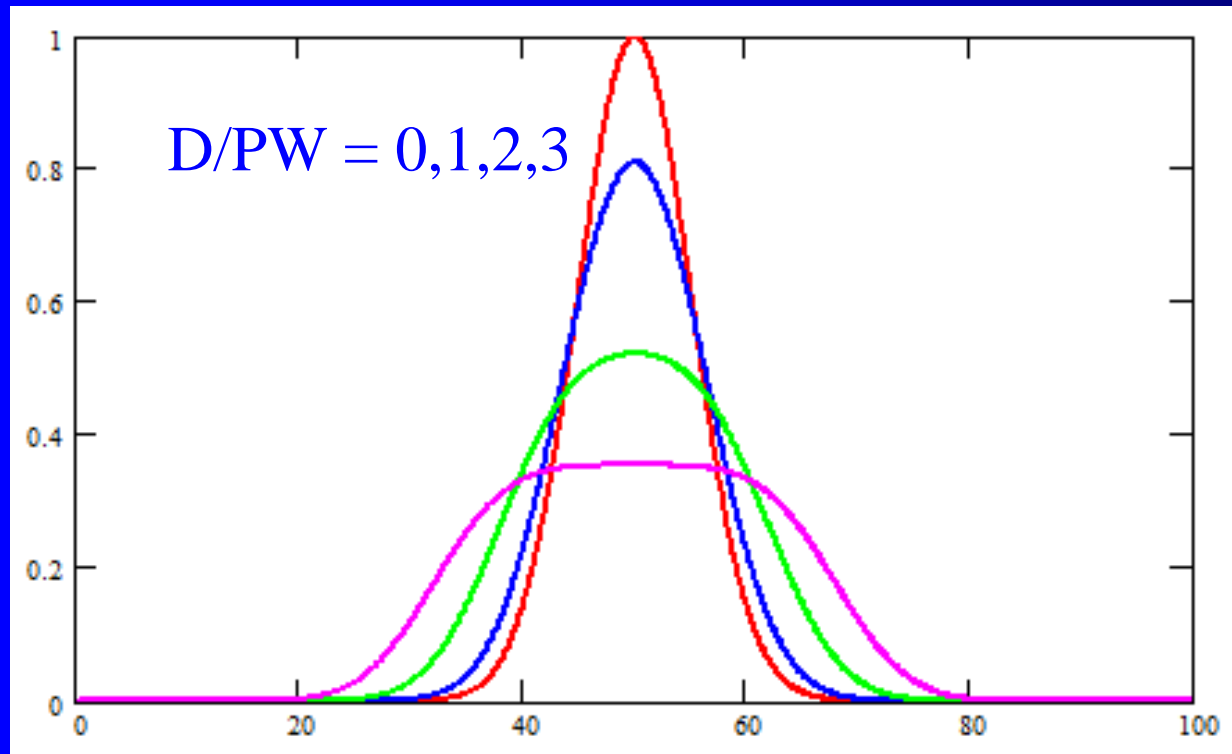
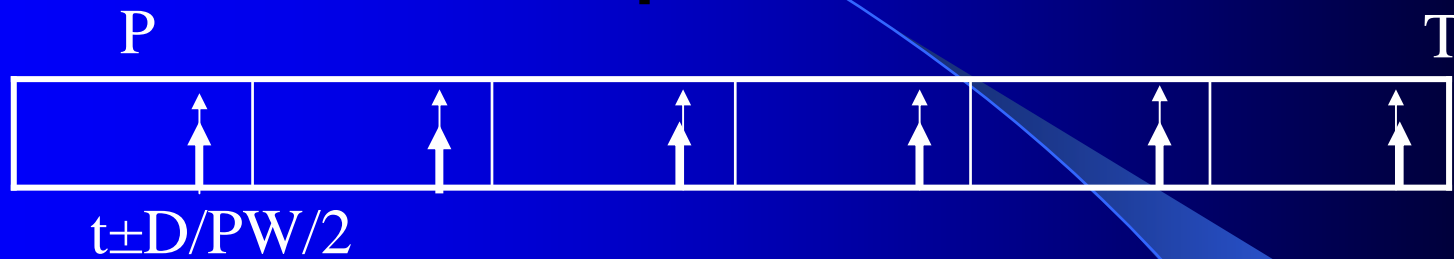
Example;  $T=7000s$   
 $p^d = -2 \cdot 10^{-10}$ ,  $P=700ms$   
Median shift =  $+3.5ms$

# Test 7 cont'd. p-dot Search Data



$$p^d = 0, -1, -2, -3 \times 10^{-10}$$

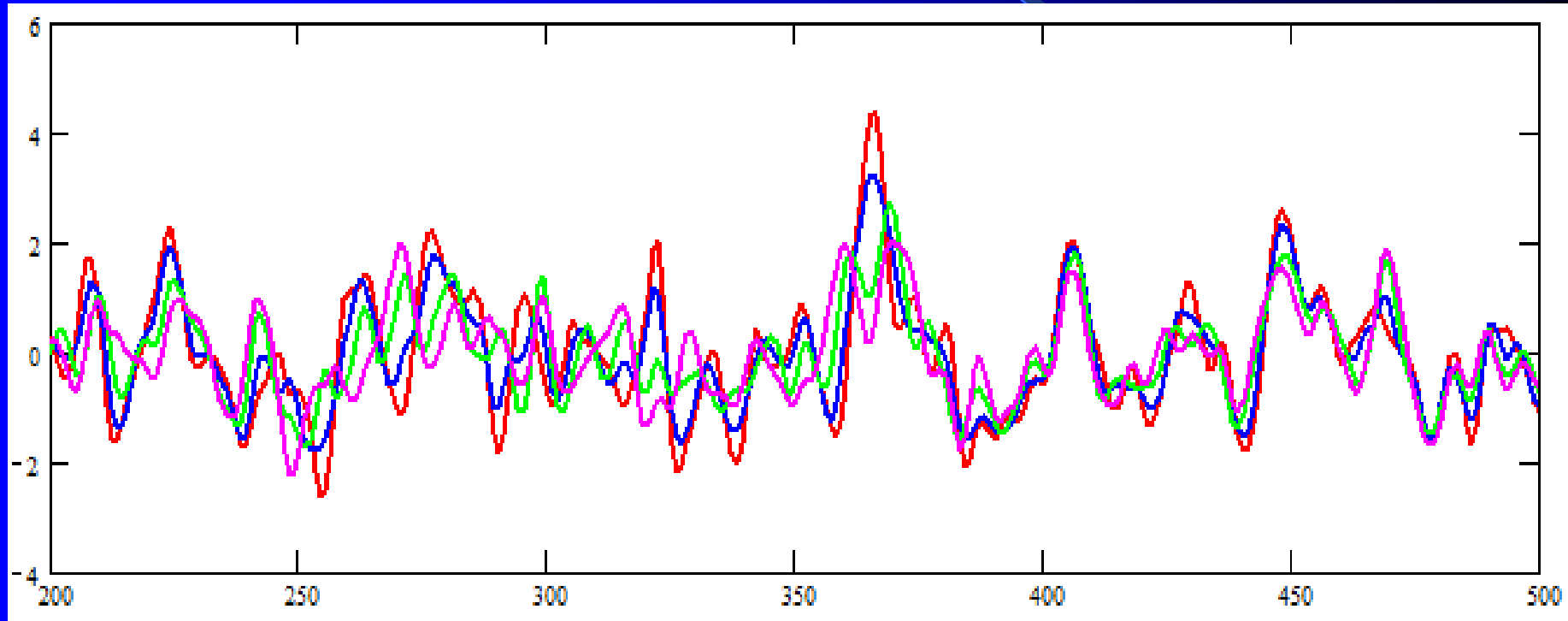
# Test 8. Dispersion Search Properties



Dispersion  
Zero at Band Centre



# Test 8 cont'd. Dispersion Search Data



$D/W = 0, \pm 1, 2, 3$  - dispersion zero at band centre

# Low SNR Validation Summary

1. Pulsar SNR's below 10:1 require careful validation
2. Interference and peaks of natural noise cause confusion
3. The key to identifying these is to exploit the pulsar properties
4. The 8-point test plan discussed works well down to 4:1 SNRs
5. In areas of low RFI some candidates are recognised down to 3:1

# Conclusions

1. Pulsar B0329 can be detected in the 300/400/600Mhz RA RF bands using home-made, small aperture ( $<2\text{m}^2$ ) antennas.
2. The main antenna design requirement is for low sidelobes.
3. Exploiting pulsar pulse properties\* is key to identifying low SNR pulsars in RFI and noise.
4. for more detail.....

*[www.ylpwe.co.uk/RAProgs/MiniPulsarRx.pdf](http://www.ylpwe.co.uk/RAProgs/MiniPulsarRx.pdf)*

\*Keith MJ et al, 'Discovery of 28 pulsars using new techniques for sorting pulsar candidates' Mon.Not. R. Astron.Soc. 395, pp837-846(2009)